Learning Tuple Probabilities in Probabilistic Databases

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Abstract

Learning the parameters of complex probabilistic-relational models from labeled training data is a standard technique in machine learning, which has been intensively studied in the subfield of Statistical Relational Learning (SRL), but—so far—this is still an under-investigated topic in the context of Probabilistic Databases (PDBs). In this paper, we focus on learning the probability values of base tuples in a PDB from query answers, the latter of which are represented as labeled lineage formulas. Specifically, we consider labels in the form of pairs, each consisting of a Boolean lineage formula and a marginal probability that comes attached to the corresponding query answer. The resulting learning problem can be viewed as the inverse problem to confidence computations in PDBs: given a set of labeled query answers, learn the probability values of the base tuples, such that the marginal probabilities of the query answers again yield in the assigned probability labels. We analyze the learning problem from a theoretical perspective, devise two optimization-based objectives, and provide an efficient algorithm (based on Stochastic Gradient Descent) for solving these objectives. Finally, we conclude this work by an experimental evaluation on three real-world and one synthetic dataset, while competing with various techniques from SRL, reasoning in information extraction, and optimization.

Keywords

Tuple-Independent Probabilistic Databases, Learning Probability Values, Stochastic Gradient Descent

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1 Introduction

The increasing availability of large, uncertain datasets, for example arising from imprecise sensor readings, information extraction or data integration applications, has led to a recent advent in the research on probabilistic databases (PDBs) [44]. PDBs adopt scalable techniques for processing queries expressed in SQL, Relational Algebra or Datalog from their deterministic counterparts. However, already for fairly simple select-project-join (SPJ) queries, computing a query answer's confidence (in the form of a marginal probability) remains a $\#\mathcal{P}$ -hard problem [10, 11]. Consequently, the majority of scientific works in this area is centered around the problem of confidence computation, either by investigating tractable subclasses of query plans [10, 11, 44], various knowledge compilation techniques [27], or general approximation techniques [35]. Moreover, nearly all the works we are aware of (except [43]) assume the probability values of base tuples stored in the PDB to be given. Although stated as a major challenge already in [8] by Dalvi, Ré and Suciu, to this date, incorporating user feedback in order to create, update, or clean a PDB has been left as future work.

Problem Setting. In this work, we address the problem of updating or cleaning a PDB by learning tuple probabilities from labeled lineage formulas. This problem can be seen as the inverse problem to confidence computations in PDBs: given a set of Boolean lineage formulas, each labeled with a probability, learn the probability values associated with the base tuples in this PDB, such that the marginal probabilities of the lineage formulas again yield their probability labels. The labels serving as input can equally result from human feedback, an application running on top of the PDB, or they can be obtained from a provided set of consistency constraints.

Related Techniques. Our work is closely related to learning the parameters (i.e., weights) of probabilistic-relational models in the field of Statistical Relational Learning (SRL) [20]. SRL comes with a plethora of individual approaches (such as Markov Logic [31, 38, 42] and the probabilistic logicprogramming engine ProbLog [13]), but due to the generality of these techniques, which are designed to support large fragments of first-order logic, it is also difficult to scale these techniques to database-like instances with millions of tuples and hundreds of thousands of labeled training data.

In this work, we focus on relational (and probabilistic) data as input and on the core operations expressible in Relational Algebra or Datalog for query processing. Moreover, we show how our approach relates to previously raised problems of deriving PDBs from incomplete databases [43] as well as of enforcing constraints over PDBs via conditioning the base tuples onto a given set of consistency constraints [30]. We illustrate our setting by the following running example.

Example 1 Our running example resembles a simple information-extraction setting, in which we employ a set of textual patterns to extract facts from various Web domains. The references to the involved patterns and the domains, as well as the extracted facts, together form the PDB shown in Figure 1.1. The fact captured by t_1 , for example, expresses that Spielberg won an Acade-

WonPrizeExtraction														
	Subject		Object			Pid		Did		p				
1	t_1 Spielberg A		AcademyAward			1		1		0.6				
ī	$t_2 \mid Spielberg \mid A$		A	AcademyAward			2 1		1		0.3			
	BornInExtraction													
	Subject		Object I		F	Pid	Did		1	D				
	t_3 Spielberg		g	Cinncinati		3		1 0		.7				
	$t_4 \mid Spielberg \mid$		LosAngeles			3	2 0		0	.4				
UsingPattern				FromDomain										
	Pid Pattern		p	Did		1	Domain			in		p		
t_5	1		Receive	ed	?	t_8	1		Wikipedia.org				?	
t_6	2		Won		?	t_9	2		Imdb.com				?	
t_7	3		Born		?									,

Figure 1.1: An Example Probabilistic Database

myAward with a given probability value of 0.6, which we consider to be provided as input to our database. In contrast, the probability values of tuples in UsingPattern and FromDomain are unknown (as indicated by the question marks). We thus are unsure about the reliability—or trustworthiness—of the extraction patterns and the Web domains that led to the extraction of our remaining facts, respectively. Learning these missing probabilities from the labeled query answers is the subject of this work.

By joining the WonPrizeExtraction relation with UsingPattern and From-Domain on Pid and Did, respectively, we can see that t_1 was extracted from Wikipedia.org using the textual pattern Received. We express this join via the following deduction rule (in Datalog-style syntax):

$$WonPrize(S,O) \leftarrow \begin{pmatrix} WonPrizeExtraction(S,O,Pid,Did) \\ \land UsingPattern(Pid,P) \\ \land FromDomain(Did,D) \end{pmatrix}$$
(1.1)

Analogously, we reconcile fact extractions for the BornIn relation as follows:

$$BornIn(S,O) \leftarrow \begin{pmatrix} BornInExtraction(S,O,Pid,Did) \\ \land UsingPattern(Pid,P) \\ \land FromDomain(Did,D) \end{pmatrix}$$
(1.2)

Instantiating (i.e., "grounding") Rules (1.1) and (1.2) against the base tuples of Figure 1.1 yields the new tuples BornIn(Spielberg, Cinncinati), BornIn(Spielberg, LosAngeles), and WonPrize(Spielberg, AcademyAward). Figure 1.2 shows these new tuples along with their Boolean lineage formulas, which capture their logical dependencies between the base tuples and the query answers derived from the two rules. A closer look at the new tuples reveals,



Figure 1.2: Example Lineages and Labels

however, that not all of them are correct. For instance, BornIn(Spielberg, LosAngeles) is wrong, so we label it with a probability of 0.0. Moreover, Won-Prize(Spielberg, AcademyAward) is likely correct, hence we label it with the probability of 0.7, as shown on top of Figure 1.2.

Given the probability labels of the query answers, the goal of the learning procedure is to learn the base tuples' unknown probability values for UsingPattern and FromDomain (while leaving the ones for WonPrizeExtraction and BornInExtraction unchanged), such that the lineage formulas again produce the given probability labels. Contributions. We summarize the contributions of this work as follows.

- To our knowledge, we present the first work to tackle the problem of learning unknown (or missing) tuple probabilities from labeled lineage formulas in the context of PDBs. In Section 4, we formally define the learning problem and analyze its properties from a theoretical perspective.
- We formulate the learning problem as an optimization problem, devise two different objective functions for solving it, and discuss both in Section 5.
- In Section 6, we present a learning algorithm based on stochastic gradient descent, which scales to problem instances with hundreds of thousands of labeled lineage formulas and millions of tuples to learn the probability values for.
- In Section 7, we show that the learning problem supports prior probabilities of base tuples which can be incorporated to update and clean PDBs. Also, we demonstrate how the learning problem relates to both learning from incomplete databases [43] and to applying constraints to PDBs [30].
- Additionally, we perform an experimental evaluation on three different real world datasets as well as on synthetic data, where we compare our approach to various techniques based on SRL, reasoning in information extraction, and optimization (Section 8).

2 Related Work

In the following, we briefly review a number of related works from the areas of SRL and PDBs, which we believe are closest to our work.

Machine Learning. Many machine learning approaches have been applied to large scale data sets (see [3] for an overview). However, the scalable methods tend to not offer a declarative language (similar to deduction rules or constraints) in order to induce correlations among facts, as queries and lineage do in PDBs. In contrast, in the subfield of SRL [20], correlations between ground atoms (similar to base tuples in PDBs) are often induced by logical formulas (similar to lineage in PDBs). But in turn, these methods lack scalability. Markov Logic Networks (MLNs) [38] (and their learning techniques [31, 42]) employ an open-world assumption, which often results in a blow-up of the grounded network structure that does not permit their application to database-like instance sizes. Even a very efficient implementation of MLNs, *Markov: TheBeast* [39], hardly meets the scalability required for typical database applications (see Section 8.3). As opposed to MLNs, *ProbLog* [13] computes marginal probabilities while relying on SLD proofs. which makes it very similar to PDBs with their closed-world assumption and deductive grounding techniques. However, also its learning procedure [24] does not scale well to large datasets (see Section 8.3). Within the ProbLog framework, [23] proposes the most similar approach to ours, however lacking both a theoretical analysis and large scale experiments.

Probabilistic Databases. A number of PDB engines, including MystiQ [7], MayBMS [2], and Trio [5] have been released as open-source prototypes in recent years and found a wide recognition in the database community. Due to the hardness of computing probabilities for query answers, a main focus of these approaches lies in finding tractable subclasses of query plans [10, 11, 44] for which probability computations can be done in polynomial time. A recent trend towards scalable inference is compiling Boolean formulas into more succinct representation formalisms such as OBDDs [27]. [9, 27], for example, develop an entire lattice of algebras and compilation techniques over unions

of conjunctive queries (UCQs) which admit for polynomial-time inference. MarkoViews [26] represent another step towards SRL, by introducing uncertain views, where probabilities depend on the input tuples, but—still—do not tackle the actual learning problem. Also, [45] circumvent the learning problem by enabling direct querying of Conditional Random Fields via a probabilistic database.

Creating Probabilistic Databases. There are very few works on the actual creation of PDBs. The authors of [43] induce a probabilistic database by estimating probabilities from a given incomplete database, a problem that is subsumed by our definition of the learning problem (see Section 7.4). Enforcing consistency constraints by conditioning [30] the base tuples of a PDB onto these constraints allows for altering the tuple probabilities (see Section 7.2). Similarly, incorporating user feedback by means of probabilistic data integration, as in [29], focuses on consistent, Boolean-only labels. Moreover, we believe that our approach has a strong application to data cleaning (see [18] for an overview) in deterministic databases, where the goal is to identify (and hence to create) a consistent database from inconsistent input data.

Lineage and Polynomials. The theoretical analysis of our learning problem (Section 4) is based on computing marginal probabilities via polynomials. The approach presented in [21] exhibits similarities to our encoding, but focuses on representing operations expressible in Relational Algebra as semiring operations over polynomials. [21] does not investigate an application of this encoding for probabilistic inference. Similarly, the authors of [21] used semirings over polynomials to model provenance, where lineage is a special case. Also, *Sum-Product Networks* [37] investigates tractable graphical models by representing these as polynomial expressions with polynomially many terms.

3 Data Model: Probabilistic Databases

In this section, we introduce our data model which follows the common possible-worlds semantics over tuple-independent probabilistic databases with data lineage [44], which has been shown to provide a *closed and complete* representation formalism for uncertain relational data [5, 44]. Throughout this section, we assume that the probabilities of all base tuples are known and fixed (i.e., even for t_5-t_9 in Example 1). Later, in Section 4 we relax this view to address the learning problem.

Probabilistic Database. We define a tuple-independent PDB [44] (\mathcal{T}, p) as a pair consisting of a finite set of base tuples \mathcal{T} and a probability measure $p: \mathcal{T} \to [0, 1]$, which assigns a probability value p(t) to each uncertain tuple $t \in \mathcal{T}$. As in a regular database, we assume the set of tuples \mathcal{T} to be partitioned into a set of extensional relations (see, e.g., WonPrizeExtraction, BornInExtraction, UsingPattern, and FromDomain in Example 1). The probability value p(t) of a base tuple t thus denotes the confidence in the existence of the tuple in the database, i.e., a higher value p(t) denotes a higher confidence in t being valid.

Possible Worlds Semantics. Assuming independence among all base tuples \mathcal{T} , the probability $P(\mathcal{W}, \mathcal{T})$ of a possible world $\mathcal{W} \subseteq \mathcal{T}$ is defined as follows.

$$P(\mathcal{W}, \mathcal{T}) := \prod_{t \in \mathcal{W}} p(t) \prod_{t \in \mathcal{T} \setminus \mathcal{W}} (1 - p(t))$$
(3.1)

In the absence of any constraints (compare to Subsection 7.2) that would restrict this set of possible worlds, any subset \mathcal{W} of tuples in \mathcal{T} forms a valid possible world (i.e., a possible instance) of the probabilistic database. Hence, there are exponentially many possible worlds.

Deduction Rules. To support query answering over a PDB, we employ deduction rules (see, e.g., Rules (1.1) and (1.2)), which we express in a Datalog-

style notation. Syntactically, these deduction rules have the shape of a logical implication with exactly one positive head literal and a conjunction of both positive and negative literals in the body. Formally, the class of rules we support corresponds to *safe*, *non-recursive* Datalog programs, which also co-incides with the core operations expressible in the Relational Algebra [1].

Definition 1 A deduction rule is a logical rule of the form

$$R(\bar{X}) \leftarrow \bigwedge_{i=1,\dots,n} R_i(\bar{X}_i) \land \bigwedge_{j=1,\dots,m} \neg R_j(\bar{X}_j) \land \Phi(\bar{X}')$$

where

- 1. R denotes the head literal's intensional relation, whereas R_i , R_j may refer to both intensional or extensional relations;
- 2. $n \ge 1$, $m \ge 0$, thus requiring at least one positive relational literal;
- 3. \bar{X} , \bar{X}_i , \bar{X}_j , and \bar{X}' denote tuples of variables and constants, where $Var(\bar{X})$, $Var(\bar{X}_j)$, $Var(\bar{X}') \subseteq \bigcup_i Var(\bar{X}_i)$;
- 4. $\Phi(\bar{X}')$ is a conjunction of arithmetic predicates, such as "=", " \neq ", and "<".

Lineage. We utilize data lineage to represent the logical dependencies between base tuples in \mathcal{T} and tuples derived from the deduction rules (see Figure 1.2). In analogy to [44], we consider lineage as a Boolean formula. It relates each derived tuple (or "query answer") with the base tuples \mathcal{T} via the three Boolean connectives \wedge , \vee and \neg , which reflect the semantics of the relational operations that were applied to derive that tuple. Specifically, we employ

- a conjunction (∧) that connects the relational literals in the body of a deduction rule;
- a negation (¬) for a negated relational literal in the body of a deduction rule;
- a disjunction (∨) whenever the same tuple is obtained from the head literals of two or more deduction rules;
- a Boolean (random) variable t representing a tuple in \mathcal{T} whenever an extensional literal matches this tuple.

For a formal definition of lineage in combination with Datalog rules and relational operators, we refer the reader to [17] and [44], respectively.

Example 2 In Figure 1.2, the conjunctions (\land) are obtained from instantiating the conjunctions in Rule (1.1) and (1.2)'s bodies. Because two instances of Rule (1.1) result in the same derived tuple WonPrize(Spielberg,AcademyAward), the disjunction (\lor) connects the two instantiated bodies. \diamond

Marginal Probabilities. We say that a possible world \mathcal{W} entails a Boolean lineage formula ϕ , denoted as $\mathcal{W} \models \phi$, if it represents a satisfying truth assignment to ϕ by setting all tuples in \mathcal{W} to true and all tuples in $\mathcal{T} \setminus \mathcal{W}$ to false. Then, we can compute the marginal probability of any Boolean formula ϕ over tuples in \mathcal{T} as the sum of the probabilities of all the possible worlds $\mathcal{W} \subseteq \mathcal{T}$ that entail ϕ :

$$P(\phi) := \sum_{\mathcal{W} \subseteq \mathcal{T}, \mathcal{W} \models \phi} \underbrace{P(\mathcal{W}, \mathcal{T})}_{\text{via Eq. (3.1)}}$$
(3.2)

To avoid the exponential cost involved in following Equation (3.2), we can—in many cases—compute the marginal probability $P(\phi)$ directly on the structure of the lineage formula ϕ [44]. Let $T(\phi) \subseteq \mathcal{T}$ denote the set of base tuples occurring in ϕ .

Definition	Condition	
P(t) := p(t)	$t \in \mathcal{T}$	
$P(\bigwedge_i \phi_i) := \prod_i P(\phi_i)$	$i \neq j \Rightarrow T(\phi_i) \cap T(\phi_j) = \emptyset$	(3.3)
$P(\bigvee_i \phi_i) := 1 - \prod_i (1 - P(\phi_i))$	$i \neq j \Rightarrow T(\phi_i) \cap T(\phi_j) = \emptyset$	(0.0)
$P(\phi \lor \psi) := P(\phi) + P(\psi)$	$\phi \wedge \psi \equiv false$	
$P(\neg\phi) := 1 - P(\phi)$		

The first line captures the case of a base tuple t, for which we return its attached probability value p(t). The next two lines handle *independent*and and *independent-or* operations for conjunctions and disjunctions over variable-disjoint subformulas ϕ_i , respectively. In the following line, we address disjunctions for two subformulas ϕ and ψ that denote disjoint probabilistic events (known as *disjoint-or* [44]). The last line finally handles negation. Equation (3.3)'s definition of $P(\phi)$ runs in linear time in the size of ϕ . However, for general Boolean formulas, computing $P(\phi)$ is $\#\mathcal{P}$ -hard [10, 44]. This becomes evident if we consider Equation (3.4), called Shannon expansion, which is a form of variable elimination that is applicable to any Boolean formula:

$$P(\phi) := p(t) \cdot P(\phi_{[t \to true]}) + (1 - p(t)) \cdot P(\phi_{[t \to false]})$$
(3.4)

Here, the notation $\phi_{[t \to true]}$ for a tuple $t \in T(\phi)$ denotes that we replace all occurrences of t in ϕ by true (and false, respectively). Repeated applications of Shannon expansions may however result in an exponential increase of ϕ . The hardness of computing $P(\phi)$ for general propositional formulas has been addressed by various techniques [44], such as knowledge compilation [27] or approximation [35].

Example 3 Consider $P((t_1 \land t_5 \land t_8) \lor (t_2 \land t_6 \land t_8))$ and assume $p(t_5) = 0.5$, $p(t_6) = 0.6$, and $p(t_8) = 0.8$ in addition to the known tuple probabilities shown in Figure 1.1. First, Line 3 of Equation (3.3) is not applicable, since t_8 occurs on both sides. So we apply a Shannon expansion, yielding $p(t_8) \cdot P((t_1 \land t_5) \lor (t_2 \land t_6)) + (1 - p(t_8)) \cdot P(false) = 0.8 \cdot P((t_1 \land t_5) \lor (t_2 \land t_6)),$ where we used P(false) = 0.0. Next, we apply Line 3 of Equation (3.3) which results in $0.8 \cdot (1 - (1 - P(t_1 \land t_5)) \cdot (1 - P(t_2 \land t_6)))$. Then, two applications of Line 2 deliver $0.8 \cdot (1 - (1 - p(t_1) \cdot p(t_5)) \cdot (1 - p(t_2) \cdot p(t_6)))$ which can be simplified to 0.3408. \diamond

Computing Marginal Probabilities via Polynomials. For the theoretical analysis of the learning problem presented in Section 4, we next devise an alternative way of computing marginals via polynomial expressions.

As a preliminary, we start from the observation that the possible worlds over a set of independent base tuples \mathcal{T} must form a probability distribution [44].

Proposition 1 For a probabilistic database (\mathcal{T},p) the possible worlds form a probability distribution:

$$\sum_{\mathcal{W}\subseteq\mathcal{T}} \underbrace{P(\mathcal{W},\mathcal{T})}_{via\ Eq.\ (3.1)} = 1$$

Proof 1 We prove the proposition by induction over the cardinality of \mathcal{T} . <u>Basis i = 1:</u> $\sum_{\mathcal{W} \subseteq \{t\}} P(\mathcal{W}, \{t_1\}) \stackrel{(3.1)}{=} p(t) + (1 - p(t)) = 1$ <u>Step $(i - 1) \rightarrow i$:</u> Let $\mathcal{T} = \{t_1, \ldots, t_i\}$, where t_i is the new tuple.

$$\sum_{\substack{(3.1)\\ = \\ \mathcal{W} \subseteq \mathcal{T}}} P(\mathcal{W}, \mathcal{T})$$

$$= \underbrace{\sum_{\mathcal{W} \subseteq \mathcal{T}} \prod_{t \in \mathcal{W}} p(t) \cdot \prod_{t \in \mathcal{T} \setminus \mathcal{W}} (1 - p(t))}_{=1} \cdot \underbrace{\sum_{w \subseteq \mathcal{T} \setminus \{t_i\}} \prod_{t \in \mathcal{W}} p(t) \cdot \prod_{t \in \mathcal{T} \setminus \mathcal{W}} (1 - p(t))}_{=1 \ by \ hypothesis}$$

Following Proposition 1, we may thus reduce the number of terms in Equation (3.2)'s sum by considering just tuples $T(\phi)$ that occur in ϕ .

Proposition 2 We can rely on tuples in $T(\phi)$, only, in order to compute $P(\phi)$ by writing:

$$P(\phi) = \sum_{V \subseteq T(\phi), V \models \phi} \underbrace{P(V, T(\phi))}_{via \ Eq. \ (3.1)}$$
(3.5)

Proof 2

$$P(\phi) = \sum_{\mathcal{W}\subseteq\mathcal{T}} \mathbf{1}_{\phi}(\mathcal{W}) \cdot P(\mathcal{W})$$

= $\left(\sum_{V\subseteq T(\phi)} \mathbf{1}_{\phi}(V) \cdot P(V)\right) \cdot \underbrace{\left(\sum_{V\subseteq(\mathcal{T}\setminus T(\phi))} P(V)\right)}_{=1 \ by \ Prop. \ 1}$

Equation (3.5) expresses $P(\phi)$ as a polynomial whose terms are defined by Equation (3.1), and the variables are p(t) for $t \in T(\phi)$. The polynomial's degree is limited as follows.

Corollary 1 A lineage formula ϕ 's marginal probability $P(\phi)$ can be expressed by a multi-linear polynomial over variables p(t), for $t \in T(\phi)$, with a degree of at most $|T(\phi)|$.

Proof 3 By inspecting Proposition 2, we note that the sum ranges over subsets of $T(\phi)$ only, hence each term has a degree of at most $|T(\phi)|$.

Example 4 Considering the lineage formula $\phi \equiv t_1 \lor t_2$, the occurring tuples are $T(\phi) = \{t_1, t_2\}$. Then, it holds that $\{t_1, t_2\} \models \phi$, $\{t_1\} \models \phi$, and $\{t_2\} \models \phi$. Hence, we can write $P(\phi) = p(t_1) \cdot p(t_2) + p(t_1) \cdot (1 - p(t_2)) + (1 - p(t_1)) \cdot p(t_2)$. Thus, $P(\phi)$ is a polynomial over the variables $p(t_1)$, $p(t_2)$ and has degree $2 = |T(\phi)| = |\{t_1, t_2\}|$.

4 Learning Problem

We now move away from the case where the probability values of all base tuples are known. Instead, we intend to learn the unknown probability values of (some of) these tuples (e.g. of t_5-t_9 in Example 1). More formally, for a tuple-independent probabilistic database (\mathcal{T}, p) , we consider $\mathcal{T}_l \subseteq \mathcal{T}$ to be the set of base tuples for which we learn their probability values. That is, initially p(t) is unknown for all $t \in \mathcal{T}_l$. Conversely, p(t) is known and fixed for all $t \in \mathcal{T} \setminus \mathcal{T}_l$. To be able to complete p(t), we are given labels in the form of pairs (ϕ_i, l_i) , each containing a lineage formula ϕ_i (i.e., a query answer) and its desired marginal probability l_i . We formally define the resulting learning problem as follows.

Definition 2 We are given a probabilistic database (\mathcal{T}, p) , a set of tuples $\mathcal{T}_l \subseteq \mathcal{T}$ with unknown probability values $p(t_l)$, for $t_l \in \mathcal{T}_l$, and a multi-set of given labels $\mathcal{L} = \langle (\phi_1, l_1), \dots, (\phi_n, l_n) \rangle$, where each ϕ_i is a lineage formula over \mathcal{T} and each $l_i \in [0, 1] \subset \mathbb{R}$ is a marginal probability for ϕ_i . Then, the learning problem is defined as follows:

Determine: $p(t_l) \in [0, 1] \subset \mathbb{R}$ for all $t_l \in \mathcal{T}_l$ such that: $P(\phi_i) = l_i$ for all $(\phi_i, l_i) \in \mathcal{L}$

Intuitively, we aim to set the probability values of the base tuples $t_l \in \mathcal{T}_l$ such that the labeled lineage formulas ϕ_i yield the marginal probability l_i . We want to remark that probability values of tuples in $\mathcal{T} \setminus \mathcal{T}_l$ remain unaltered. Also, we note that the Boolean labels *true* and *false* can be represented as $l_i = 0.0$ and $l_i = 1.0$, respectively. Hence, Boolean labels resolve to a special case of Definition 2's labels.

Example 5 Formalizing Example 1's problem setting, we obtain $\mathcal{T} := \{t_1, \ldots, t_9\}, \mathcal{T}_l := \{t_5, \ldots, t_9\}$ with labels $((t_1 \wedge t_5 \wedge t_8) \vee (t_2 \wedge t_6 \wedge t_8), 0.7)$, and $((t_3 \wedge t_7 \wedge t_9), 0.0)$.

Unfortunately, the above problem definition exhibits hard instances. First, computing $P(\phi_i)$ may be $\#\mathcal{P}$ -hard [10], which would require many Shannon expansions. But even for cases when all $P(\phi_i)$ can be computed in polynomial time (i.e., when Equation (3.3) is applicable), there are combinatorially hard cases of the above learning problem.

Lemma 1 For a given instance of Definition 2's learning problem, where all $P(\phi_i)$ with $(\phi_i, l_i) \in \mathcal{L}$ can be computed in polynomial time, deciding whether there exists a solution to the learning problem is \mathcal{NP} -hard.

Proof 4 We encode the 3-satisfiability problem (3SAT) for a Boolean formula $\Psi \equiv \psi_1 \wedge \cdots \wedge \psi_n$ in CNF into Definition 2's learning problem. For each variable $X_i \in Var(\Psi)$, we create two tuples t_i, t'_i whose probability values will be learned. Hence, $2 \cdot |Var(\Psi)| = |\mathcal{T}_i| = |\mathcal{T}|$. Then, for each X_i , we add the label $((t_i \wedge t'_i) \vee (\neg t_i \wedge \neg t'_i), 1.0)$. The corresponding polynomial equation $p(t_i)p(t'_i) + (1 - p(t_i))(1 - p(t'_i)) = 1.0$ has exactly two possible solutions for $p(t_i), p(t'_i) \in [0, 1]$, namely $p(t_i) = p(t'_i) = 1.0$ and $p(t_i) = p(t'_i) = 0.0$. Next, we replace all variables X_i in Ψ by their tuple t_i . Now, for each clause ψ_i of Ψ , we introduce one label $(\psi_i, 1.0)$. Altogether, we have $|\mathcal{L}| = |Var(\Psi)| + n$ labels for Definition 2's problem. Each labeled lineage formula ϕ has at most three variables, hence $P(\phi)$ takes at most 8 steps. Still, Definition 2 solves 3SAT, where the learned values of each pair of $p(t_i), p(t'_i)$ (either 0.0 or 1.0) correspond to X_i 's truth value for a satisfying assignment of Ψ . From this, it follows that the decision problem formulated in Lemma 1 is \mathcal{NP} -hard.

Moreover, from Lemma 1 it follows that finding a solution to Definition 2's learning problem is \mathcal{FNP} -hard (see [36]).

Besides computationally hard instances, there might also be *inconsistent* instances of the learning problem. That is, it may be impossible to define $p: \mathcal{T}_l \to [0, 1]$ such that all labels are satisfied.

Example 6 If we consider $\mathcal{T}_l := \{t_1, t_2\}$ with labels $\mathcal{L} := \langle (t_1, 0.2), (t_2, 0.3), (t_1 \wedge t_2, 0.9) \rangle$, then it is impossible to fulfill all three labels at the same time.

From a practical point of view, there remain a number of questions regarding Definition 2. First, how many labels do we need in comparison to the number of tuples for which we are learning the probability values (i.e., $|\mathcal{L}|$ vs. $|\mathcal{T}_l|$)? And second, is there a difference in labeling lineage formulas that involve many tuples or very few tuples (i.e., $|T(\phi_i)|$)?

These questions will be addressed by the following theorem. It is based on Corollary 1's computation of marginal probabilities via their polynomial representation. We write the learning problem's conditions $P(\phi_i) = l_i$ as polynomials over variables $p(t_l)$ of the form $P(\phi_i) - l_i$, where $t_l \in \mathcal{T}_l$ and the probability values p(t) for all $t \in \mathcal{T} \setminus \mathcal{T}_l$ are fixed and hence represent constants.

Theorem 1 If the labeling is consistent, Definition 2's problem instances can be classified as follows:

- 1. If $|\mathcal{L}| < |\mathcal{T}_l|$, the problem has infinitely many solutions.
- 2. If $|\mathcal{L}| = |\mathcal{T}_l|$ and the polynomials $P(\phi_i) l_i$ have common zeros, then the problem has infinitely many solutions.
- 3. If $|\mathcal{L}| = |\mathcal{T}_l|$ and the polynomials $P(\phi_i) l_i$ have no common zeros, then the problem has at most $\prod_i |T(\phi_i) \cap \mathcal{T}_l|$ solutions.
- 4. If $|\mathcal{L}| > |\mathcal{T}_l|$, then the polynomials $P(\phi_i) l_i$ have common zeros, thus reducing this to one of the previous cases.

Proof 5 The first case is a classical under-determined system of equations. In the second case, without loss of generality, there are two polynomials $P(\phi_i) - l_i$ and $P(\phi_j) - l_j$ with a common zero, say $p(t_k) = c_k$. Setting $p(t_k) = c_k$ satisfies both $P(\phi_i) - l_i = 0$ and $P(\phi_j) - l_j = 0$, hence we have $\mathcal{L}' := \mathcal{L} \setminus \langle (\phi_i, l_i), (\phi_j, l_j) \rangle$ and $\mathcal{T}'_l := \mathcal{T}_l \setminus \{t_k\}$ which yields the theorem's first case again $(|\mathcal{L}'| < |\mathcal{T}'_l|)$. Regarding the third case, Bezout's theorem [14], a central result from algebraic geometry, is applicable: for a system of polynomial equations, the number of solutions (including their multiplicities) over variables in \mathbb{C} is equal to the product of the degrees of the polynomials. In our case, the polynomials are $P(\phi_i) - l_i$ with variables $p(t_l), t_l \in \mathcal{T}_l$. So, according to Corollary 1 their degree is at most $|T(\phi_i) \cap \mathcal{T}_l|$. Since our variables $p(t_l) \cap \mathcal{T}_l|$ is an upper bound on the number of solutions. In the fourth case, the system of equations is over-determined, such that redundancies like common zeros will reduce the problem to one of the previous cases.

Example 7 We illustrate the theorem by providing examples for each of the four cases.

- 1. In Example 5's formalization of Example 1, we have $|\mathcal{T}_l| = 5$ and $|\mathcal{L}| = 2$. So, the problem is under-specified and has infinitely many solutions, since assigning $p(t_7) = 0.0$ enables $p(t_9)$ to take any value in $[0, 1] \subset \mathbb{R}$.
- 2. We assume $\mathcal{T}_l = \{t_5, t_6, t_7\}$, and $\mathcal{L} = \langle (t_5 \land \neg t_6, 0.0), (t_5 \land \neg t_6 \land t_7, 0.0), (t_5 \land t_7, 0.0) \rangle$. This results in the equations $p(t_5) \cdot (1 p(t_6)) = 0.0, p(t_5) \cdot (1 p(t_6)) = 0.0$.

 $(1-p(t_6)) \cdot p(t_7) = 0.0$, and $p(t_5) \cdot p(t_7) = 0.0$, where $p(t_5)$ is a common zero to all three polynomials. Hence, setting $p(t_5) = 0.0$ allows $p(t_6)$ and $p(t_7)$ to take any value in $[0, 1] \subset \mathbb{R}$.

- 3. Let us consider $\mathcal{T}_l = \{t_7, t_8\}$.
 - (a) If $\mathcal{L} = \langle (t_7, 0.4), (t_8, 0.7) \rangle$, then there is exactly one solution as predicted by $|T(t_7)| \cdot |T(t_8)| = 1$.
 - (b) If $\mathcal{L} = \langle (t_7 \wedge t_8, 0.1), (t_7 \vee t_8, 0.6) \rangle$, then there are two solutions, namely $p(t_7) = 0.2$, $p(t_8) = 0.5$ and $p(t_7) = 0.5$, $p(t_8) = 0.2$. Here, $\prod_i |T(\phi_i) \cap \mathcal{T}_i| = |T(t_7 \wedge t_8)| \cdot |T(t_7 \vee t_8)| = 4$ is an upper bound.
- 4. We extend this example's second case by the label $(t_5, 0.0)$, thus yielding the same solutions but having $|\mathcal{L}| > |\mathcal{T}_l|$.

In general, a learning problem instance has many solutions, where Definition 2 does not specify a precedence, but all of them are equivalent. The number of solutions shrinks by adding labels to \mathcal{L} , or by labeling lineage formulas ϕ_i that involve fewer tuples in \mathcal{T}_l (thus resulting in a smaller intersection $|T(\phi_i) \cap \mathcal{T}_l|$). Hence, to achieve more uniquely specified probabilities for all tuples $t_l \in \mathcal{T}_l$, in practice we should obtain the same number of labels as the number of tuples for which we learn their probability values, i.e., $|\mathcal{L}| = |\mathcal{T}_l|$, and label those lineage formulas with fewer tuples in \mathcal{T}_l .

Based on algebraic geometry, the learning problem allows for an interesting visual interpretation. All possible definitions of probability values for tuples in \mathcal{T}_l , that is $p : \mathcal{T}_l \to [0, 1]$, span the hypercube $[0, 1]^{|\mathcal{T}_l|}$. In Example 7, Cases 3(a) and 3(b), the hypercube has two dimensions, namely $p(t_7)$ and $p(t_8)$, as depicted in Figures 4.1(a) and 4.1(b). Hence, one definition of pspecifies exactly one point in the hypercube. Moreover, all definitions of pthat satisfy a given label define a curve (or plane) through the hypercube (e.g., the two labels in Figure 4.1(a) define two straight lines).

Moreover, also the points, in which all labels' curves intersect, represent solutions to the learning problem (e.g., the solutions of Example 7, Case 3(b), are the intersections in Figure 4.1(b)). If the learning problem is inconsistent, there is no point in which all labels' curves intersect. Furthermore, if the learning problem has infinitely many solutions, the labels' curves intersect in curves or planes, rather than points.



Figure 4.1: Visualization of the Learning Problem

5 Solving the Learning Problem

In the previous section, we formally characterized the learning problem and devised the basic properties of its solutions. From a visual perspective, Definition 2 established curves and planes whose intersections represent the solutions (see, e.g., Figure 4.1(b)). In this section, we introduce different objective functions that describe surfaces whose optima correspond to these solutions. For instance, Figure 4.1(b)'s problem has Figure 4.1(c)'s surface if we the use mean squared error (MSE) as the objective, which will be defined in this section. Calculating a gradient on such a surface thus allows the application of an optimization method to solve the learning problem.

Alternative Approaches. In general, based on the polynomial equations, an exact solution to an instance of the learning problem can be computed in exponential time [14], which is not acceptable in a database setting. Also, besides gradient-based optimization methods, other approaches, such as expectation maximization [22], are possible and represent valuable targets for future work.

Partial Derivative of a Lineage Formula. In order to establish a gradient on Definition 2's conditions, i.e., $P(\phi_i) = l_i$, we introduce the partial derivative of a lineage formula's marginal probability $P(\phi)$ with respect to a given tuple $t \in T(\phi)$.

Definition 3 [28] Given a lineage formula ϕ and a tuple $t \in T(\phi)$, the partial derivative of $P(\phi)$ with respect to p(t) is defined as:

$$\frac{\partial P(\phi)}{\partial p(t)} := P(\phi_{[t \to true]}) - P(\phi_{[t \to false]})$$

Here, $\phi_{[t \to true]}$ means that all occurrences of t in ϕ are replaced by true (and analogously for *false*). A formal justification for the above definition is provided in [28].

Example 8 Considering the marginal probability $P(t_1 \vee t_2)$ with $p(t_1) = 0.6$, we determine the partial derivative with respect to $p(t_2)$, that is $\frac{\partial P(t_1 \vee t_2)}{\partial p(t_2)} = P(t_1 \vee true) - P(t_1 \vee false) = 1.0 - 0.6 = 0.4$.

Desired Properties for Solving the Learning Problem. Before we define objective functions for solving the learning problem, we establish a list of desired properties of these (which we do not claim to be complete). Later, we judge different objectives based on these properties.

Definition 4 An objective function to the learning problem should satisfy the following three desired properties:

- 1. All instances of Definition 2's learning problem can be expressed, including inconsistent ones.
- 2. If all $P(\phi_i)$ are computable in polynomial time, then also the objective is computable in polynomial time.
- 3. The objective is stable, that is $\mathcal{L} := \langle (\phi_1, l_1), \ldots, (\phi_n, l_n) \rangle$ and $\mathcal{L} \cup \langle (\phi'_i, l_i) \rangle$ with $\phi'_i \equiv \phi_i, (\phi_i, l_i) \in \mathcal{L}$ define the same surface.

Here, the first case ensures that the objective can be applied to all instances of the learning problem. We insist on inconsistent instances, because they occur often in practice (see Figure 8.1(a)). The second property restricts a blow-up in computation, which yields the following useful characteristic: if we can compute $P(\phi)$ for all labels, e.g., for labeled query answers, then we can also compute the objective function. Finally, the last of the desiderata reflects an objective function's ability to detect dependencies between labels. Since $\phi_i \equiv \phi'_i$ both \mathcal{L} and $\mathcal{L} \cup \langle (\phi'_i, l_i) \rangle$ allow exactly the same solutions, the surface should be the same. Unfortunately, including convexity of an objective as an additional desired property is not possible. For example Figure 4.1(b) has two disconnected solutions, which induce at least two optima, thus prohibiting convexity. In the following, we establish two objective functions, which behave very differently with respect to the desired properties.

5.1 Logical Objective

If we restrict the learning problem's probability labels to $l_i \in \{0.0, 1.0\}$, we can define a objective function based on computing marginals as follows.

Definition 5 Let an instance of Definition 2's learning problem be given by a probabilistic database (\mathcal{T}, p) , tuples with unknown probability values $\mathcal{T}_l \subseteq \mathcal{T}$, and labels $\mathcal{L} = \langle (\phi_1, l_1), \ldots, (\phi_n, l_n) \rangle$ such that all $l_i \in \{0.0, 1.0\}$. Then, the logical objective is formulated as:

$$Logical(\mathcal{L}, p) := P\left(\bigwedge_{(\phi_i, l_i) \in \mathcal{L}, l_i = 1.0}^{} \phi_i \wedge \bigwedge_{(\phi_i, l_i) \in \mathcal{L}, l_i = 0.0}^{} \neg \phi_i\right)$$
(5.1)

The above definition is a maximization problem, and its global optima are identified by $Logical(\mathcal{L}, p) = 1.0$. Moreover, from Definition 3, we may obtain its derivative.

Example 9 Let $\mathcal{T} = \mathcal{T}_l := \{t_1, t_2\}$ and $\mathcal{L} := \langle (t_1 \lor t_2, 1.0), (t_1, 0.0) \rangle$ be given. Then, $Logical(\mathcal{L}, p)$ is instantiated as $P((t_1 \lor t_2) \land \neg t_1) = P(\neg t_1 \land t_2)$. Visually, this defines a surface whose optimum lies in $p(t_1) = 0.0$ and $p(t_2) = 1.0$, as shown in Figure 4.1(d).

With respect to Definition 4, the third desired property is fulfilled, as $P(\phi'_i \land \phi_i) = P(\phi_i)$. Hence, the logical objective's surface, shown for instance in Figure 4.1(d), is never altered by adding equivalent labels. Still, the first property is not given, since the probability labels are restricted to $l_i \in \{0.0, 1.0\}$ and inconsistent problem instances collapse Equation (5.1) to P(false), thus rendering the objective non-applicable. Also, the second property is violated, because in the spirit of Lemma 1's proof, we can construct an instance where each label's $P(\phi_i)$ on its own is computable in polynomial time, whereas the computation of the marginal probability for Equation (5.1) is $\#\mathcal{P}$ -hard.

5.2 Mean-Squared-Error Objective

Another approach, which is common in machine learning, lies in using the mean squared error (MSE) to define the objective function.

Definition 6 Let an instance of Definition 2's learning problem be given by a probabilistic database (\mathcal{T}, p) , tuples with unknown probability values $\mathcal{T}_l \subseteq \mathcal{T}$, and labels $\mathcal{L} = \langle (\phi_1, l_1), \ldots, (\phi_n, l_n) \rangle$. Then, the mean-squared-error objective function is formulated as:

$$MSE(\mathcal{L}, p) := \frac{1}{|\mathcal{L}|} \sum_{(\phi_i, l_i) \in \mathcal{L}} (P(\phi_i) - l_i)^2$$

Moreover, its partial derivative with respect to the tuple's probability value p(t) is:

$$\frac{\partial MSE(\mathcal{L}, p)}{\partial p(t)} := \frac{1}{|\mathcal{L}|} \sum_{(\phi_i, l_i) \in \mathcal{L}, t \in T(\phi_i)} 2 \cdot (P(\phi_i) - l_i) \cdot \underbrace{\frac{\partial P(\phi_i)}{\partial p(t)}}_{\text{Def. 3}}$$

The above formulation is a minimization problem whose solutions have 0.0 as the objective's value.

Example 10 Example 7, Case 3(b), is visualized in Figure 4.1(b). The corresponding surface induced by the MSE objective is depicted in Figure 4.1(c) and has its minima at the learning problem's solutions. \diamond

Judging the above objective by means of Definition 4, we realize that the first property is met, as there are no restrictions on the learning problem, and inconsistent instances can be tackled (but deliver objective values larger than zero). Furthermore, since the $P(\phi_i)$'s occur in separate terms of the objective's sum, the second desired property is maintained. However, the third desired property is violated, as illustrated by the following example.

Example 11 In accordance to Example 9 and Figure 4.1(d), we set $\mathcal{T} = \mathcal{T}_l := \{t_1, t_2\}$ and $\mathcal{L} := \langle (t_1 \lor t_2, 1.0), (t_1, 0.0) \rangle$. Then, the MSE objective defines the surface in Figure 4.1(e). However, if we replicate the label $(t_1, 0.0)$, thus resulting in Figure 4.1(f) (note the "times two" in the objective), its surface becomes steeper along the $p(t_1)$ -axis, but has the same minimum. Thus, MSE's surface is not stable. Instead, it becomes more ill-conditioned [34].

5.3 Discussion

Both the logical objective and the MSE objective have optima exactly at the solutions of Definition 2's learning problem. With respect to Definition 4's desired properties, we summarize the behavior of both objectives in the following table:

	Properties				
Objective	1.	2.	3.		
Logical	×	×	\checkmark		
MSE	\checkmark	\checkmark	×		

The two objectives satisfy opposing desired properties, and it is certainly possible to define other objectives behaving similarly to one of them. Unfortunately, there is little hope for an objective that is adhering to all three properties. The second property inhibits computational hardness. However, Lemma 1 and the third property's logical tautology checking (i.e., $\models \phi_i \leftrightarrow \phi'_i$, which is co- \mathcal{NP} -complete) require these. In this regard the logical objective addresses both computationally hard problems by computing marginals, whereas the MSE objective avoids them.

In the remainder of the paper, we will favor the MSE objective, as it is more practical. In reality, many learning problem instances are inconsistent or have non-Boolean labels (see Figure 8.1(a)), and Equation (5.1)'s marginal computations are often too expensive (see Section 8.6).

6 Learning Algorithm

Given a learning problem's surface (see, e.g., Figure 4.1(c)), as it is defined by the choice of the objective function, the learning algorithm provided in this section determines how to move over this surface in order to reach an optimum, that is, to find a solution to the learning problem.

Learning Algorithm. Our learning algorithm is based on stochastic gradient descend (SGD) [6], which we here demonstrate to scale to instance sizes with millions of tuples and hundreds of thousands of labels (see Section 8.5). It is initialized at a random point and repeatedly moves into the direction of a partial derivative until convergence. Visually, we start at a random point (e.g., somewhere in Figure 4.1(c)), and then in each step we move in parallel to an axis (e.g., $p(t_1)$ or $p(t_2)$), until we reach an optimum.

In Algorithm 1 best, represents the objective's best known value, where p holds the corresponding probability values of tuples in \mathcal{T}_l . Also, η_l is the learning rate, which exists and may differ for each tuple in \mathcal{T}_l . Line 4's loop is executed until convergence to the absolute error bound of ϵ_{abs} . Then, Line 5 shuffles the order of \mathcal{T}_l 's tuples for the inner loop of Line 6. Within each iteration, Line 8 updates one tuple's probability value, which yields the updated definition p' of p. If p' is an improvement over p with respect to the objective (as verified in Line 11), we assign p' to p and double the tuple's learning rate η_l . Otherwise, p' is discarded, and the learning rate η_l is halved.

Example 12 We execute Algorithm 1 on Figure 4.1(e)'s example. Following Definition 6 the corresponding partial derivatives are:

$$\frac{\partial MSE}{\partial p(t_1)} := (P(t_1 \lor t_2) - 1.0) \cdot (P(true \lor t_2) - P(false \lor t_2)) \\
+ (P(t_1) - 0.0) \cdot (P(true) - P(false)) \\
\frac{\partial MSE}{\partial p(t_2)} := (P(t_1 \lor t_2) - 1.0) \cdot (P(t_1 \lor true) - P(t_1 \lor false))$$
(6.1)

Assuming that Line 1 delivers $p(t_1) = 0.7$ and $p(t_2) = 0.5$, we get best = $(-0.15)^2 + (0.7)^2 \approx 0.512$ in Line 3. If $\epsilon_{abs} = 0.01$ we enter Line 4's loop,

Algorithm 1 Learning($(\mathcal{T}, p), \mathcal{T}_l, \mathcal{L}, \epsilon_{abs}$)

Input: Probabilistic database (\mathcal{T}, p) , tuples \mathcal{T}_l to learn the probability values for, labeled lineage formulas \mathcal{L} , error bound ϵ_{abs} **Output:** p with learned probability values, best value of objective 1: $\forall t_l \in \mathcal{T}_l : p(t_l) := Rand(0, 1)$ \triangleright Random initialization 2: $\forall t_l \in \mathcal{T}_l : \eta_l := 1.0$ \triangleright Per-tuple learning rate 3: $best := MSE(\mathcal{L}, p)$ \triangleright Definition 6 4: while $best > \epsilon_{abs}$ do 5:sequence := $Shuffle(\mathcal{T}_l)$ \triangleright Permuted sequence while $\neg IsEmpty(sequence)$ do 6: 7: $t_l := Pop(sequence)$ \triangleright Get first element $p'(t_l) := p(t_l) - \eta_l \cdot \frac{\partial MSE(\mathcal{L},p)}{\partial n(t_l)}$ 8: \triangleright Definition 6 9: $p' := p \cup \{p'(t_l)\}$ 10: $newVal := MSE(\mathcal{L}, p')$ \triangleright Definition 6 if newVal < best then 11: 12: $\eta_l := 2 \cdot \eta_l$ \triangleright Increase t_l 's learning rate p := p' \triangleright Keep new value of $p(t_l)$ 13:best := newVal14:else 15: $\eta_l := \frac{1}{2} \cdot \eta_l$ 16: \triangleright Decrease t_l 's learning rate

17: return p, best

where Line 5 randomly orders t_2 before t_1 . Then, $p(t_2)$'s partial derivative evaluates as follows $\frac{\partial MSE}{\partial p(t_2)}\Big|_{(0.7,0.5)} = (0.85 - 1.0) \cdot (1.0 - 0.7) = -0.055$. Since $\eta_2 = 1.0$, we get $p'(t_2) = 0.5 - (-0.055) = 0.555$ in Line 8. Hence, in Line 10, newVal = $(-0.1335)^2 + 0.7^2 \approx 0.508$. As 0.508 < 0.512, Line 11's condition turns true, such that we get $\eta_2 = 2.0$, $p(t_1) = 0.7$, $p(t_2) = 0.555$ and best = 0.508. Hence, in further iterations the increased η_2 speeds up movements along $p(t_2)$'s partial derivative. \diamond

Tackling MSE's Instability. The disadvantage of the MSE objective is that it does not satisfy Definition 4's third desired property. We argue, that Algorithm 1 counters to some extent the instability, which we illustrate by the following example.

Example 13 Let us evaluate the gradient of Figures 4.1(e) and 4.1(f) in the point $p(t_1) = p(t_2) = 0.5$. Following Equation (6.1), we obtain the gradient (0.375, -0.125) for Figure 4.1(e). Analogously, Figure 4.1(f) has (0.875, -0.125). Even although both figures show the same minimum, the gradients differ heavily in $p(t_1)$'s partial derivative. \diamond

Inspecting the above example, we note that the gradient is indeed affected, but each partial derivative on its own points into the correct direction, i.e. increasing $p(t_2)$ and decreasing $p(t_1)$. Hence, weighting the partial derivatives can counter the effect. We achieve this by keeping one learning rate η_l per tuple and adapting them during runtime. In Section 8.4, we empirically show a superior convergence over a global learning rate. Previously, the authors of [31] also reported speed ups in ill-conditioned instances by introducing separate learning rates per dimension.

Implementation Issues. In this paragraph, we briefly describe four implementation issues, which were omitted in Algorithm 1 for presentation purposes. First, Line 4's absolute error bound is inconvenient, because the optima of inconsistent learning problem instances have an MSE value larger than 0.0. Therefore, we use both an absolute error bound ϵ_{abs} and a relative error bound ϵ_{rel} . Second, since their marginal probabilities $P(\phi_i)$ are repeatedly computed, it is beneficial to preprocess the lineage formulas ϕ_i , e.g. by compiling them to OBDDs [27], or by flattening them via a few targeted Shannon expansions [16], the latter of which we also apply in this work. Next, Line 8 might yield a probability value that exceeds the interval [0, 1], which we counter by the *logit* function. It defines a mapping from probability values in [0, 1] to $\mathbb{R} \cup \{\pm \infty\}$. **Definition 7** The logit function transforms a probability $p \in [0,1]$ to a weight $w \in \mathbb{R} \cup \{\pm \infty\}$ as follows:

$$w = \ln \frac{p}{1.0 - p}$$
 $p = \frac{1}{1 + \exp(-w)}$

Example 14 If p = 0.5, then w = 0.0. Also p = 1.0 implies $w = +\infty$, whereas p = 0.0 yields $w = -\infty$.

Hence, we calculate with weights in $\mathbb{R} \cup \{\pm \infty\}$, rather than on probability values in [0, 1]. Finally, if two tuples $t_l, t'_l \in \mathcal{T}_l$ are disjoint with respect to the labels' lineage formulas they occur in, that is $\{\phi_i \mid (\phi_i, l_i) \in \mathcal{L}, t_l \in T(\phi_i), t'_l \in T(\phi_i)\} = \emptyset$, then their probability values can be updated in parallel.

Alternative Approaches. Due to its various applications, there is an entire zoo of gradient-based optimization techniques [34]. Approaches, such as Newton's method, which are based on the Hessian, do not to scale to database-like instance sizes. This disadvantage is circumvented by Quasi-Newton methods, for instance limited-memory Broyden-Fletcher-Goldfarb-Shanno (L-BFGS) [34], which estimates the Hessian. We empirically compare our approach to L-BFGS and plain gradient descent in Section 8.4.

Algorithm Properties. Algorithm 1 comes with three properties, which we share with all alternative approaches we are aware of, including other gradient-based methods and expectation maximization [22]. First, the algorithm is *non-deterministic*, which is caused by Lines 1 and 5. Second, gradient-based optimization methods, including Algorithm 1, can get stuck in *local optima*, which is nevertheless hard to avoid in non-convex problems. In this regard, the non-determinism is a potential advantage, since restarting the algorithm will yield varying solutions, thus increasing the chance for finding a global optimum. Finally, the solutions returned by Algorithm 1 for the MSE objective are *not exact*, but rather very close to an optimum, which however can be controlled by the error bounds ϵ_{rel} and ϵ_{abs} . Additional experiments on these aspects are available in the Appendix of this report.

7 Extensions and Applications

In this section, we briefly investigate how the learning problem can be extended by priors (Section 7.1), how it relates to conditioning PDBs via constraints (Section 7.2), how these constraints can be employed to update or clean PDBs (Section 7.3), and how it relates to handling incompleteness in databases (Section 7.4).

7.1 Prior Probabilities

In order to explicitly incorporate preferences in the form of prior probabilities of base tuples $t_l \in \mathcal{T}_l$ into our learning objective (instead of just considering them to be "unknown"), we can extend Definition 6's MSE objective as follows.

Definition 8 Given a function prior : $\mathcal{T}_l \to [0,1] \subset \mathbb{R}$, Definition 6's MSE objective function can be extended to

$$\frac{c}{|\mathcal{L}|} \cdot \sum_{(\phi_i, l_i) \in \mathcal{L}} (P(\phi_i) - l_i)^2 + \frac{1 - c}{|\mathcal{T}_l|} \cdot \sum_{t_l \in \mathcal{T}_l} (P(t_l) - prior(t_l))^2$$

where $c \in [0, 1]$ is a constant.

Utilizing c, we can control the trade-off between the impact of the lineage labels and the *prior* function.

Expressiveness. Definition 8 is not more general than the original MSE objective. We can express priors in Definition 6 by creating a label $(t_l, prior(t_l))$ for each tuple $t_l \in \mathcal{T}_l$, which then produces $\sum_{t_l \in \mathcal{T}_l} (P(t_l) - prior(t_l))^2$ also in Definition 6's objective. The coefficients preceding the sums can be emulated by replicating labels in \mathcal{L} . Thus, priors are a special case of lineage labels.

7.2 Constraints and Conditioning

Conditioning by Learning. Considering constraints in the form of propositional formulas over a probabilistic database's tuples, we can encode each constraint ϕ_i with the label (ϕ_i , 1.0) into an instance of the learning problem.

Lemma 2 Given a probabilistic database (\mathcal{T}, p) and constraints in the form of propositional formulas ϕ_1, \ldots, ϕ_n over \mathcal{T} , whose conjunction $\phi_1 \wedge \cdots \wedge \phi_n$ is satisfiable. Then, if we create a learning problem instance by setting $\mathcal{T}_l := \mathcal{T}$ and $\mathcal{L} := \langle (\phi_1, 1.0), \ldots, (\phi_n, 1.0) \rangle$, its solution p' conditions the probabilistic database (\mathcal{T}, p) with respect to ϕ_1, \ldots, ϕ_n . Hence, for a propositional query ψ over (\mathcal{T}, p') it holds, that:

$$P(\psi \mid \phi_1 \land \dots \land \phi_n) = P(\psi)$$

Proof 6 We observe that in the learning problem's solution p', we get $P(\phi_1 \land \dots \land \phi_n) = 1.0$. Moreover, over (\mathcal{T}, p') , we can rewrite the marginal probability of a query answer ψ as follows.

$$P(\psi) \stackrel{(3.2)}{=} \sum_{\mathcal{W} \subseteq \mathcal{T}, \models \psi} P(\mathcal{W}, \mathcal{T}) = \sum_{\mathcal{W} \subseteq \mathcal{T}, \mathcal{W} \models \psi, \mathcal{W} \models \phi_1, \dots, \mathcal{W} \models \phi_n} P(\mathcal{W}, \mathcal{T}) = P(\psi \land \phi_1 \land \dots \land \phi_n)$$

By combining both equations, we obtain over (\mathcal{T}, p') :

$$P(\psi \mid \phi_1 \land \dots \land \phi_n) = \frac{P(\psi \land \phi_1 \land \dots \land \phi_n)}{P(\phi_1 \land \dots \land \phi_n)} = \frac{P(\psi)}{1.0} = P(\psi)$$

Thus, the solution to the learning problem can be seen as a form of applying conditioning [30] to a PDB. From a Bayesian perspective, the solution to the learning problem p' can be seen as posterior probabilities of the base tuples in \mathcal{T}_l . However, unlike the approach presented in [30], we do not materialize and store the constraints along with the result tuples.

Learning by Conditioning. Following Definition 5's logical objective, we can apply constraint-enforcing approaches to solve a subset of possible learning problem instances. The subset is characterized by instances with consistent labels, having $\mathcal{T} = \mathcal{T}_l$, and by restricting the lineage labels to $l_i \in \{0.0, 1.0\}$. We create a single constraint in the form of Equation (5.1)'s conjunction, initially set all tuple confidences to 0.5, and solve the resulting conditioning problem [30].

7.3 Updating and Cleaning PDBs

Updating. If we are given an existing probabilistic database (\mathcal{T}, p) and knowledge in the form of labeled lineage formulas $\mathcal{L} := \langle (\phi_1, l_1), \ldots, (\phi_n, l_n) \rangle$, we can update the tuples' probability values via the learning problem. We produce a new probabilistic database (\mathcal{T}, p') , whose probability values p' are updated according to the information provided in \mathcal{L} . To achieve this, we create a learning problem instance (whose solution is p') by using \mathcal{L} , setting $\mathcal{T}_l := \mathcal{T}$ and defining a prior prior(t) := p(t).

Cleaning. The new probability values p' allow for cleaning the probabilistic database as follows. If p' defines a tuple's probability value to be 0.0, we can delete it from the database. Conversely, if p' yields 1.0 for a tuple's probability value, we can move it into a new, deterministic relation.

7.4 Incomplete Databases

A field that is related to PDBs are incomplete databases. Intuitively, in an incomplete database, some attributes values or entire tuples may be missing in the given database instance. A completion of an incomplete database can be seen as a possible world in a PDB—with a probability.

Missing Attribute Values. In [43], a PDB is derived from an incomplete database which exhibits missing attributes in some of its tuples. Their idea is to estimate the probability of a possible completion of an incomplete tuple from the complete part of the database. We show that this approach is an instance of the learning problem via the following reduction.

Let an incomplete database be given by a set of complete tuples \mathcal{T}_c and a set of incomplete tuples \mathcal{T}_i . We consider an incomplete tuple $R(\bar{a}) \in \mathcal{T}_i$ of relation R, where one or more attributes in \bar{a} lack values, such that all possible completions are represented by $\bar{a}_i \supseteq \bar{a}$ (assuming finite domains). Then, we create a new uncertain relation $R' := \{\bar{a}_i \mid \bar{a}_i \supseteq \bar{a}\}$ and add one deduction rule per completion \bar{a}_i :

$$R(\bar{a}_i) \leftarrow R'(\bar{a}_i) \land \bigwedge_{j \neq i} \neg R'(\bar{a}_j)$$

The above rules allow at most one completion of \bar{a} to be true within a possible world, so the resulting lineage formulas form a block-independent PDB [44]. Now, we create labels following [43]'s approach. For a subset of argument values $\bar{s} \subset \bar{a}$, we count how often the complete tuples \mathcal{T}_c feature the completion \bar{a}_i , in symbols $I_{\bar{s}}(\bar{a}_i) := |\{R(\bar{a}') \in \mathcal{T}_c \mid \bar{a} \cap \bar{a}' = \bar{s}, \bar{a}_i \setminus \bar{a} \subset \bar{a}'\}|$. Then, for each completion \bar{a}_i , we generate the label $(R(\bar{a}_i), \frac{I_{\bar{s}}(\bar{a}_i)}{\sum_j I_{\bar{s}}(\bar{a}_j)})$. Besides these labels, the resulting learning problem instance uses the new relations R''s tuples in \mathcal{T}_l .

Missing Tuples. Generally, any database instance can be seen as a finite subset of the crossproduct of its attributes' domains. We now consider an incomplete database, whose (finite sets of) existing tuples and potentially missing tuples are \mathcal{T}_c and \mathcal{T}_m , respectively. Assume we intend to enforce logical formulas ϕ_1, \ldots, ϕ_n over tuples $\mathcal{T}_c \cup \mathcal{T}_m$, which could for example result from constraints or user feedback. We create a learning problem instance by setting $\mathcal{T} := \mathcal{T}_c \cup \mathcal{T}_m$, $\mathcal{T}_l := \mathcal{T}_m$ and $\mathcal{L} := \langle (\phi_1, 1.0), \ldots, (\phi_n, 1.0) \rangle$. Thus, a solution to the learning problem will complete \mathcal{T}_c with (possibly uncertain) tuples from \mathcal{T}_m , such that the logical formulas ϕ_1, \ldots, ϕ_n are fulfilled.

8 Experiments

Our evaluation focuses on the following four aspects. First, we compare the quality of our approach to learning techniques in SRL (Section 8.1) and to constraint-based reasoning techniques applied in information extraction settings (Section 8.2). Second, we compare the runtime behavior of our algorithm to SRL methods (Section 8.3) and to other gradient-based optimization techniques (Section 8.4). Third, we explore the scalability of our method to large data sets (Section 8.5). Finally, in Section 8.6, we investigate the runtime behavior of the two objective functions defined in Section 5. Due to space constraints, additional experiments on varying ϵ_{abs} , ϵ_{rel} and Algorithm 1's ability to find global optima are available in Appendix A.

Overview. As an overview, we present the basic characteristics of all learning problem instances in Figure 8.1(a), where Avg. $T(\phi)$ is calculated as $\frac{1}{|\mathcal{L}|} \sum_{(\phi_i, l_i) \in \mathcal{L}} |T(\phi_i)|$.

Setup. Our engine is implemented in Java. It employs a PostgreSQL 8.4 database backend for evaluating Datalog rules in a bottom-up manner and to instantiate lineage formulas. If not stated otherwise, *PDB* refers to Algorithm 1's implementation with the MSE objective and a per-tuple learning rate. For checking convergence, we set $\epsilon_{abs} = 10^{-6}$ and $\epsilon_{rel} = 10^{-4}$. We ran all experiments on an 8-core Intel Xeon 2.4GHz machine with 48 GB RAM, repeated each setting four times, and report the average of the last three runs. Whenever different programs compete, all of them run in single-threaded mode. All rules used in the experiments are provided in Appendix A.

8.1 Quality Task: SRL Setting

Dataset. We use the openly available UW-CSE dataset¹, which comprises a database describing the University of Washington's computer science depart-

¹http://alchemy.cs.washington.edu/data/uw-cse/

ment via the following relations: AdvisedBy, CourseLevel, HasPosition, In-Phase, Professor, ProjectMember, Publication, Student, TaughtBy, Ta (teaching assistant), and YearsInProgram. Moreover, the dataset is split into five sub-departments, and we consider this dataset's relations to be deterministic.

Task. The goal is inspired by an experiment in [38], namely to predict the AdvisedBy relation from all input relations except *Student* and *Professor*. We train and test in a leave-one-out fashion by sub-department.

Rules. We automatically create 49 rules resembling all joins (including self-joins) between two relations (except *student*, *professor*, and *AdvisedBy*), having at least one argument of type person. Furthermore, we add one uncertain relation *rules*, containing one tuple for each of the 49 rules and include the corresponding tuple in the join, for example:

$$AdvisedBy(P_1, P_2) \leftarrow \begin{pmatrix} Ta(D, C, P_1, T) \land \\ TaughtBy(D, C, P_2, T) \land \end{pmatrix}$$

The remaining rules are provided in Appendix A. We learn the probability values of the 49 tuples, hence classifying how well each rule predicts the AdvisedBy relation.

Labels. Regarding labels, we used the 113 instances of AdvisedBy as positive labels, i.e., all their probability labels are 1.0. In addition, there are about 16,000 person-person pairs not contained in AdvisedBy. We randomly draw pairs from these as negative labels (with a probability label of 0.0).

SRL Competitors. We compete with *TheBeast* [39], the fastest Markov Logic [38] implementation we are aware of. It uses an in-memory database and performs inference via Integer Linear Programming. We ran it on the same set of data and rules. Additionally, we ran the probabilistic Prolog engine *ProbLog* [24], but even on the reduced datasize of one sub-department it did not terminate after one hour.

Results. In Figure 8.1(b), we depict both the runtimes as well as the prediction quality in terms of the F_1 measure (the harmonic mean of precision and recall) for the *AdvisedBy* relation. *TheBeast* is a straight line, since it allows only positive labels. For *PDB*, we started with all positive labels and added increasing numbers of negative labels.

Analysis. Regarding runtimes, PDB is consistently about 40 times faster than *TheBeast*. With respect to F_1 , adding more negative labels to PDB yields improvements until we saturate at the same level as *TheBeast*.
8.2 Quality Task: Information Extraction

Dataset. This dataset² contains about 450,000 crawled web pages in the sports and celebrities domains, where about 12,500 textual patterns are used to extract facts.

Task. Following [46], we consider two different relations, namely *WorksFor-Club* in the sports domain and *IsMarriedTo* in the celebrities domain. Both relations contain facts with temporal annotations. The goal is to determine, for each textual pattern, whether it expresses a temporal *begin*, *during* or *end* event of one of the two relations, or none of them. For example, for *WorksForClub*, we could find that David Beckham joined Real Madrid in 2003 (*begin*), scored goals for them in 2005 (*during*), and left the club in 2007 (*end*).

PDB Setup. We model temporal data in the PDB according to [16]. Text occurrences of a potential fact are stored in the deterministic relation Occurrence(Pid, E1, E2, Types, Begin, End), where Types holds the entities' types and Begin, End contain integers encoding the limits of their occurrences' time intervals. To encode the decision whether a pattern expresses a temporal begin, during, or end event, we instantiate three uncertain relations Begin(Pid), During(Pid), and End(Pid), which each hold one entry per pattern and whose probability values we learn. Text occurrences of potential facts are connected to the patterns by six rules (see Appendix A for details) of the following kind

 $Is Married To Begin(E_1, E_2, T_1, T_2) \\ \leftarrow Begin(Pid) \land Occurrence(Pid, E_1, E_1, pp, T_1, T_2)$

where pp stands for person-person type pair. To enforce that a textual pattern expresses at most one of *begin*, *during*, or *end*, we make them mutually exclusive via the rules

Constraint1(Pid)	\leftarrow	$Begin(Pid) \land During(Pid)$
Constraint2(Pid)	\leftarrow	$Begin(Pid) \wedge End(Pid)$
Constraint3(Pid)	\leftarrow	$During(Pid) \wedge End(Pid)$

whose resulting lineage formulas we label with 0.0. Moreover, we use temporal precedence constraints by instantiating six rules of the form

 $\begin{aligned} & Is Married To Begin(E_1, E_2, T_1, T_2) \land \\ & Constraint (E_1, E_2) \leftarrow Is Married To During(E_1, E_2, T_3, T_4) \\ & \land T_3 < T_2 \end{aligned}$

² http://www.mpi-inf.mpg.de/yago-naga/pravda/

and label their lineage with 0.0. Finally, we employ the 266 labels for textual patterns and the 341 labels for facts from the original work [46].

Competitor. The authors of [46] utilized a combination of Label Propagation and Integer Linear Programming to rate the textual patterns and to enforce temporal constraints.

Results. In Figure 8.1(c), we report our system's (PDB) result along with the best result from [46] (PRAVDA). To evaluate precision, we sampled 100 facts per relation and event type and annotated them manually. Recall is the absolute number of facts obtained.

Analysis. For relations with a few, decisive textual patterns, *PDB* keeps up with precision, while slightly gaining in recall, probably due to the relaxation of constraints by the MSE objective. However, for *worksForClub*'s *during* relation, there is a vast number of relevant patterns, which puts Label Propagation's undirected model in favor, whereas our directed model suffers in terms of recall.

8.3 Runtime Task: SRL Methods

Setup. To systematically verify scalability, we create synthetic data sets as follows. We fix $\mathcal{T} = \mathcal{T}_l$ to 100 tuples. Then, we instantiate a growing number of lineage formulas of the form $(t \land \neg t \land \neg t) \lor (t \land \neg t \land \neg t)$, where all tuple identifiers are uniformly drawn from \mathcal{T}_l , and negations exist with probability 0.5. Each formula's probability label is randomly set to either 0.0 or 1.0.

Competitors. Besides *TheBeast* [39], we compete with *ProbLog* [24], a probabilistic Prolog engine, whose grounding techniques and distribution semantics are closest to ours.

Results. For each value of $|\mathcal{L}|$, we create five problem instances and depict their average runtime in Figure 8.1(d).

Analysis. *PDB* converges on average about 600 times faster than *ProbLog* and about 70 times faster than *TheBeast*.

8.4 Runtime Task: Gradient Methods

Setup. We employ the openly available YAGO2³ knowledge base, which comprises about 110 relations. The task is to learn the probability values of tuples \mathcal{T}_l in the *LivesIn* relation. Moreover, we label the following rule's

 $ToLabel(L) \leftarrow LivesIn(P,L)$

 $^{^{3} \}rm http://www.mpi-inf.mpg.de/yago-naga/yago/$

lineage formulas with synthetic target probabilities. Since the rule's projection on the first argument makes all lineage formulas ϕ disjoint with respect to their tuples $T(\phi)$, the resulting learning problem instance is consistent. Hence, its global optima have a mean squared error (MSE) of 0.0.

Competitors. Algorithm 1 with per tuple learning rate (SGD Per-Tuple) competes with a single learning rate (SGD Single), with gradient descent (GD), and with L-BFGS [34], which approximates the Hessian with its second derivatives. All methods are initialized with the same learning rate.

Results. We plot the MSE against the runtime of the different methods in Figure 8.1(e).

Analysis. GD takes less time per iteration. Hence its curves drops faster in the beginning, but then stagnates. The two SGD variants behave similarly at first. Later on, the per-tuple learning rate yields constant improvements, whereas the single learning rate does not. *L-BFGS*, finally, improves slowly in comparison.

8.5 Runtime Task: Scalability

Dataset. As previously, we run on YAGO2³. For tuples in $\mathcal{T} \setminus \mathcal{T}_l$, we use uniformly drawn synthetic probability values.

Labels. In order to create labels, we run queries on YAGO2 and label their answers' lineage formulas with synthetic target probabilities (see Appendix A for details).

Results. Figure 8.1(f) contains the results of three large learning problem instances P1 to P3, where *Init* is the time spent on instantiating the lineage formulas, and *Algorithm 1* had multi-threading enabled.

Analysis. The *Init* time is determined by the number $(|\mathcal{L}|)$ and size (Avg. $T(\phi)$) of lineage formulas being instantiated. Algorithm 1 is faster on consistent instances (P3). Its runtime is dominated by the number of labels per tuple $t_l \in \mathcal{T}_l$.

8.6 Runtime Task: Objectives

Setup. As a last experiment, we run Algorithm 1 once with the *Logical* objective (see Definition 5) and once with the mean-squared-error (MSE) objective (see Definition 6). The synthetic data is created analogously to Section 8.3.

Results & Analysis. Already on tiny instances of up to 15 labels as in Figure 8.1(g), the *Logical* objective slows down significantly in comparison to MSE, due to the expensive marginal computations of Equation (5.1).

Section	Figure	Source	$ \mathcal{T} $	$ \mathcal{T}_l $	$ \mathcal{L} $	Avg. $T(\phi)$	Boolean	Incons.
8.1	8.1(b)	$UW-CSE^1$	2,161	49	113 to 452	5.8 to 8.3	yes	yes
8.2	8.1(c)	PRAVDA ²	75,091	37,383	89,874	2.3	no	yes
8.3	8.1(d)	synthetic	100	100	10 to 100	5.8	yes	yes
8.4	8.1(e)	$YAGO2^3$	224,440,854	19,985	5,562	3.6	no	no
8.5	8.1(f) P1			217,846	228,050	2.7	no	yes
8.5	8.1(f) P2	$YAGO2^3$	224,440,854	217,846	79,600	60.6	no	yes
8.5	8.1(f) P3			1,721,156	459, 597	3.7	no	no
8.6	8.1(g)	synthetic	100	100	1 to 15	5.8	yes	no
	(a) Dataset Statistics							



milliseconds



Figure 8.1: Experimental Results

9 Conclusions

We introduced a novel method for learning tuple confidences in tuple-independent PDBs. We analyzed the properties of this learning problem from a theoretical perspective, devised gradient-based solutions, investigated the relationship to other problems, and presented an implementation together with extensive experiments. For future work, we see numerous promising directions. Studying tractable subclasses of the learning problem or dropping the tuple-independence assumption would improve our theoretical understanding. Other valuable targets lie in the creation of a large, publicly available benchmark and the application of the learning problem to a broader range of related problems, e.g., inspired by the ones in Section 7.

Appendix A Rules and Constraints

This appendix contains a detailed description of the deduction rules and consistency constraints we applied for Section 8 of this report.

A.1 Quality Task: SRL Data

We set $\mathcal{T} := CourseLevel \cup HasPosition \cup InPhase \cup Professor \cup Project Member \cup Publication \cup Student \cup TaughtBy \cup Ta \cup YearsInProgram \cup Rules and <math>\mathcal{T}_l := Rules$. Here, Rules is the only uncertain relation. The 49 automatically created rules are:

$$\begin{aligned} AdvisedBy(P_1, P_2) \leftarrow \begin{pmatrix} Ta(D, C, P_1, Te) \land Rules(0) \\ Ta(D, C, P_2, Te) \land Rules(0) \end{pmatrix} \\ AdvisedBy(P_1, P_2) \leftarrow \begin{pmatrix} Ta(D, C, P_1, Te) \land Rules(1) \\ TaughtBy(D, C, P_2, Te) \land Rules(1) \end{pmatrix} \\ AdvisedBy(P_1, P_2) \leftarrow \begin{pmatrix} Ta(D, C, P_1, Te) \land Rules(2) \\ Publication(D, Ti, P_2) \land Rules(2) \end{pmatrix} \\ AdvisedBy(P_1, P_2) \leftarrow \begin{pmatrix} Ta(D, C, P_1, Te) \land Rules(3) \\ YearsInProgram(D, P_2, Y) \land Rules(3) \end{pmatrix} \\ AdvisedBy(P_1, P_2) \leftarrow \begin{pmatrix} Ta(D, C, P_1, Te) \land Rules(4) \\ HasPosition(D, P_2, Po) \land Rules(4) \end{pmatrix} \\ AdvisedBy(P_1, P_2) \leftarrow \begin{pmatrix} Ta(D, C, P_1, Te) \land Rules(5) \\ InPhase(D, P_2, Ph) \land Rules(5) \end{pmatrix} \\ AdvisedBy(P_1, P_2) \leftarrow \begin{pmatrix} Ta(D, C, P_1, Te) \land Rules(5) \\ InPhase(D, P_2, Ph) \land Rules(5) \end{pmatrix} \end{aligned}$$

$AdvisedBy(P_1, P_2) \leftarrow \Big($	$ \begin{array}{c} TaughtBy(D, C, P_1, Te) \land \\ Ta(D, C, P_2, Te) \land \end{array} Rules(7) \end{array} \right) $
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$TaughtBy(D, C, P_1, Te) \land TaughtBy(D, C, P_2, Te) \land Rules(8)$
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$\begin{array}{c} TaughtBy(D, C, P_1, Te) \land \\ Publication(D, Ti, P_2) \land \end{array} Rules(9) \end{array}$
$AdvisedBy(P_1, P_2) \leftarrow \Big($	$\frac{TaughtBy(D, C, P_1, Te) \wedge}{YearsInProgram(D, P_2, Y) \wedge} Rules(10) \right)$
$AdvisedBy(P_1, P_2) \leftarrow \Big($	$\begin{array}{c} TaughtBy(D, C, P_1, Te) \land \\ HasPosition(D, P_2, Po) \land \end{array} Rules(11) \end{array}$
$AdvisedBy(P_1, P_2) \leftarrow \Big($	$\frac{TaughtBy(D, C, P_1, Te) \land}{InPhase(D, P_2, Ph) \land} Rules(12)$
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$\begin{array}{c} TaughtBy(D, C, P_1, Te) \land \\ ProjectMember(D, Pr, P_2) \land \end{array} Rules(13) \end{array}$
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$\frac{Publication(D, Ti, P_1) \land}{Ta(D, C, P_2, Te) \land} Rules(14) $
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$\frac{Publication(D, Ti, P_1) \land}{TaughtBy(D, C, P_2, Te) \land} Rules(15)$
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$\begin{array}{c} Publication(D, Ti, P_1) \land \\ Publication(D, Ti, P_2) \land \end{array} Rules(16) \end{array}$
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$\begin{array}{c} Publication(D, Ti, P_1) \land \\ YearsInProgram(D, P_2, Y) \land \end{array} Rules(17) \end{array} \right)$
$AdvisedBy(P_1, P_2) \leftarrow \Big($	$\begin{array}{c}Publication(D, Ti, P_1) \land \\HasPosition(D, P_2, Po) \land \end{array} Rules(18)\end{array}$
$AdvisedBy(P_1, P_2) \leftarrow \Big($	$\frac{Publication(D, Ti, P_1) \land}{InPhase(D, P_2, Ph) \land} Rules(19)$
$AdvisedBy(P_1, P_2) \leftarrow \Big($	$\begin{array}{c} Publication(D, Ti, P_1) \land \\ ProjectMember(D, Pr, P_2) \land \end{array} Rules(20) \end{array}$
$AdvisedBy(P_1, P_2) \leftarrow \Big($	$\frac{YearsInProgram(D, P_1, Y) \land}{Ta(D, C, P_2, Te) \land} Rules(21) \right)$
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$\begin{array}{l} YearsInProgram(D, P_1, Y) \land \\ TaughtBy(D, C, P_2, Te) \land \end{array} Rules(22) \end{array} \right)$
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$\begin{array}{c} YearsInProgram(D, P_1, Y) \land \\ Publication(D, Ti, P_2) \land \end{array} Rules(23) \end{array}$
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$YearsInProgram(D, P_1, Y) \land YearsInProgram(D, P_2, Y) \land Rules(24) $
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$YearsInProgram(D, P_1, Y) \land Rules(25) $ HasPosition(D, P_2, Po) \land
$AdvisedBy(P_1, P_2) \leftarrow \Big($	$\frac{YearsInProgram(D, P_1, Y) \land}{InPhase(D, P_2, Ph) \land} Rules(26) \right)$

$AdvisedBy(P_1, P_2) \leftarrow \Big($	$\frac{YearsInProgram(D, P_1, Y) \land}{ProjectMember(D, Pr, P_2) \land} Rules(27) \right)$
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$ \begin{array}{c} HasPosition(D, P_1, Po) \land \\ Ta(D, C, P_2, Te) \land \end{array} Rules(28) \end{array} \right) $
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$HasPosition(D, P_1, Po) \land Rules(29) $ TaughtBy(D, C, P_2, Te) $\land Rules(29) $
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$\begin{array}{c} HasPosition(D, P_1, Po) \land \\ Publication(D, Ti, P_2) \land \\ \end{array} Rules(30) \end{array}$
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$ \begin{array}{c} HasPosition(D, P_1, Po) \land \\ YearsInProgram(D, P_2, Y) \land \end{array} Rules(31) \end{array} \right) $
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$ \begin{array}{c} HasPosition(D, P_1, Po) \land \\ HasPosition(D, P_2, Po) \land \\ HasPosition(D, Po) \land \\ HasPosition(D,$
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$\frac{HasPosition(D, P_1, Po) \land}{InPhase(D, P_2, Ph) \land} Rules(33) \end{pmatrix}$
$AdvisedBy(P_1, P_2) \leftarrow \left\langle \right\rangle$	$HasPosition(D, P_1, Po) \land ProjectMember(D, Pr, P_2) \land Rules(34)$
$AdvisedBy(P_1, P_2) \leftarrow \left\langle \right\rangle$	$ \frac{InPhase(D, P_1, Ph) \land}{Ta(D, C, P_2, Te) \land} Rules(35)\right) $
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$ \frac{InPhase(D, P_1, Ph) \land}{TaughtBy(D, C, P_2, Te) \land} \frac{Rules(36)}{Rules(36)} $
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$ \frac{InPhase(D, P_1, Ph) \land}{Publication(D, Ti, P_2) \land} Rules(37)\right) $
$AdvisedBy(P_1, P_2) \leftarrow \left\langle \right\rangle$	$InPhase(D, P_1, Ph) \land YearsInProgram(D, P_2, Y) \land Rules(38) $
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$ \frac{InPhase(D, P_1, Ph) \land}{HasPosition(D, P_2, Po) \land} \frac{Rules(39)}{Rules(39)} $
$AdvisedBy(P_1, P_2) \leftarrow \left\langle \right\rangle$	$ \frac{InPhase(D, P_1, Ph) \wedge}{InPhase(D, P_2, Ph) \wedge} Rules(40) \\ Lu Phase(D, P_2, Ph) \wedge Rules(40) \\ $
$AdvisedBy(P_1, P_2) \leftarrow \left\langle \right\rangle$	$ \frac{InPhase(D, P_1, Ph) \land}{ProjectMember(D, Pr, P_2) \land} Rules(41) \\ \xrightarrow{Rules(41)} \\ \xrightarrow{Rules(41)}$
$AdvisedBy(P_1, P_2) \leftarrow \left\langle \right\rangle$	$\frac{ProjectMember(D, Pr, P_1) \land}{Ta(D, C, P_2, Te) \land} Rules(42) $
$AdvisedBy(P_1, P_2) \leftarrow \left\langle \right\rangle$	$\frac{ProjectMember(D, Pr, P_1) \land}{TaughtBy(D, C, P_2, Te) \land} Rules(43)$
$AdvisedBy(P_1, P_2) \leftarrow \left(\right)$	$\frac{ProjectMember(D, Pr, P_1) \land}{Publication(D, Ti, P_2) \land} Rules(44) \end{pmatrix}$
$AdvisedBy(P_1, P_2) \leftarrow \Big($	$\frac{ProjectMember(D, Pr, P_1) \land}{YearsInProgram(D, P_2, Y) \land} Rules(45) \right)$

$$\begin{aligned} AdvisedBy(P_1, P_2) \leftarrow \begin{pmatrix} ProjectMember(D, Pr, P_1) \land \\ HasPosition(D, P_2, Po) \land \\ ProjectMember(D, Pr, P_1) \land \\ InPhase(D, P_2, Ph) \land \\ AdvisedBy(P_1, P_2) \leftarrow \begin{pmatrix} ProjectMember(D, Pr, P_1) \land \\ ProjectMember(D, Pr, P_1) \land \\ ProjectMember(D, Pr, P_2) \land \\ ProjectMember(D, Pr, P_2) \land \\ \end{pmatrix} \end{aligned}$$

Regarding the variables, D is a department name, P_1 and P_2 are persons, C is a course, Po is a position, Te is a term, Ph is a phase, Pr is a project, Ti is a title, and Y is a year.

Finally, positive labels (label probability 1.0) are from the actual instances of the AdvisedBy relation. Negative labels (label probability 0.0) are uniformly drawn person-person pairs not present in AdvisedBy.

A.2 Quality Task: Fact Extraction

We set $\mathcal{T} := Occurrence \cup Begin \cup During \cup End$ and $\mathcal{T}_l := Begin \cup During \cup End$. Also, *Occurrence* is certain, whereas the other three relations are uncertain. There are three types of rules. First, for reconciling facts we have

```
\begin{split} &IsMarriedToBegin(E_1, E_2, T_1, T_2) \\ &\leftarrow Begin(Pid) \land Occurrence(Pid, E_1, E_1, pp, T_1, T_2) \\ &IsMarriedToDuring(E_1, E_2, T_1, T_2) \\ &\leftarrow During(Pid) \land Occurrence(Pid, E_1, E_1, pp, T_1, T_2) \\ &IsMarriedToEnd(E_1, E_2, T_1, T_2) \\ &\leftarrow End(Pid) \land Occurrence(Pid, E_1, E_1, pp, T_1, T_2) \\ &WorksForClubBegin(E_1, E_2, T_1, T_2) \\ &\leftarrow Begin(Pid) \land Occurrence(Pid, E_1, E_1, pc, T_1, T_2) \\ &WorksForClubDuring(E_1, E_2, T_1, T_2) \\ &\leftarrow During(Pid) \land Occurrence(Pid, E_1, E_1, pc, T_1, T_2) \\ &WorksForClubEnd(E_1, E_2, T_1, T_2) \\ &\leftarrow During(Pid) \land Occurrence(Pid, E_1, E_1, pc, T_1, T_2) \\ &WorksForClubEnd(E_1, E_2, T_1, T_2) \\ &\leftarrow End(Pid) \land Occurrence(Pid, E_1, E_1, pc, T_1, T_2) \\ \end{array}
```

where E_1 and E_2 are entities, T_1 and T_2 are integers representing time interval limits, *PId* is the pattern id, and *pp* and *pc* are constants standing for the type pairs person-person and person-club, respectively. The next rules enforce mutual exclusion

by labeling their resulting lineage with probability 0.0. Finally, we encode temporal precedence constraints by the rules

$$Constraint4(E_1, E_2) \leftarrow \begin{pmatrix} IsMarriedToBegin(E_1, E_2, T_1, T_2) \land \\ IsMarriedToDuring(E_1, E_2, T_3, T_4) \land \\ T_3 < T_2 \end{pmatrix}$$

$$Constraint5(E_1, E_2) \leftarrow \begin{pmatrix} IsMarriedToBegin(E_1, E_2, T_1, T_2) \land \\ IsMarriedToEnd(E_1, E_2, T_3, T_4) \land \\ T_3 < T_2 \end{pmatrix}$$

$$Constraint6(E_1, E_2) \leftarrow \begin{pmatrix} IsMarriedToDuring(E_1, E_2, T_1, T_2) \land \\ IsMarriedToEnd(E_1, E_2, T_3, T_4) \land \\ T_3 < T_2 \end{pmatrix}$$

$$Constraint7(E_1, E_2) \leftarrow \begin{pmatrix} WorksForClubBegin(E_1, E_2, T_1, T_2) \land \\ WorksForClubDuring(E_1, E_2, T_3, T_4) \land \\ T_3 < T_2 \end{pmatrix}$$

$$Constraint8(E_1, E_2) \leftarrow \begin{pmatrix} WorksForClubBegin(E_1, E_2, T_1, T_2) \land \\ WorksForClubBegin(E_1, E_2, T_3, T_4) \land \\ T_3 < T_2 \end{pmatrix}$$

$$Constraint9(E_1, E_2) \leftarrow \begin{pmatrix} WorksForClubDuring(E_1, E_2, T_1, T_2) \land \\ WorksForClubDuring(E_1, E_2, T_3, T_4) \land \\ T_3 < T_2 \end{pmatrix}$$

whose resulting lineage we label by probability 0.0 as well. Additionally, we use the 266 labels for textual patterns and the 341 labels for facts from the original work.

A.3 Runtime Task: SRL Methods

We synthetically set $\mathcal{T} = \mathcal{T}_l := \{t_0, \ldots, t_{99}\}$ which are all uncertain tuples. Then, we create a growing number of synthetic rule pairs following the pattern

$$Head(c) \leftarrow t_i \land \neg t_j \land \neg t_k$$
$$Head(c) \leftarrow t_l \land \neg t_m \land \neg t_n$$

such that c is a constant indicating the rule id, and i, j, k, l, m, n are uniformly drawn random numbers from $0, \ldots, 99$, and displayed negations exist with probability 0.5. Now, we uniformly draw a synthetic probability label from $\{0.0, 1.0\}$ for Head(c)'s lineage.

A.4 Runtime Task: Gradient Methods

We set \mathcal{T} to be all of YAGO2's relations and $\mathcal{T}_l := LivesIn$. All relations are uncertain, where tuples in $\mathcal{T} \setminus \mathcal{T}_l$ have synthetic probability values uniformly drawn from [0, 1]. The only rule we have is

 $ToLabel(P) \leftarrow LivesIn(P, L)$

whose resulting lineage formulas we label by synthetic probabilities uniformly drawn from [0, 1].

A.5 Runtime Task: Scalability

We set \mathcal{T} to be all of YAGO2's relations. All relations are uncertain, where tuples in $\mathcal{T} \setminus \mathcal{T}_l$ have synthetic probability values uniformly drawn from [0, 1]. **P1.** Here, $\mathcal{T}_l := ActedIn \cup WasBornIn$ and the rules are

 $\begin{array}{l} Movie(M) \leftarrow ActedIn(P, M) \\ Creator(P) \leftarrow ActedIn(P', M) \land Created(P, M) \\ Location(L) \leftarrow WasBornIn(P, L) \\ Person(P) \leftarrow WasBornIn(P, L) \\ Person2(P) \leftarrow WasBornIn(P, L) \land IsLocatedIn(L, L') \end{array}$

whose resulting lineage formulas have synthetic probability labels uniformly drawn from [0, 1].

P2. Here, $\mathcal{T}_l := ActedIn \cup WasBornIn$ and the rules are

```
\begin{aligned} &Movie(M) \leftarrow ActedIn(P, M) \\ &Actor(P) \leftarrow ActedIn(P, M) \land Created(P', M) \\ &Location(L) \leftarrow WasBornIn(P, L) \\ &Person(P) \leftarrow WasBornIn(P, L) \land LivesIn(P', L) \end{aligned}
```

whose resulting lineage formulas have synthetic probability labels uniformly drawn from [0, 1].

P3. Here, $\mathcal{T}_l := IsLocatedIn_Transitive$ and the only rule is

 $Location(L) \leftarrow IsLocatedIn_Transitive(L, L')$

whose resulting lineage formulas have synthetic probability labels uniformly drawn from [0, 1].

A.6 Runtime Task: Objectives

The setup is described in detail in Section 8.6.

Appendix B Additional Experiments

In this appendix, we provide additional experiments on the convergence of the MSE objective for varying error rates as well as on its tendency to converge to a global optimum. First, we vary the error rates ϵ_{rel} and ϵ_{abs} to investigate their impact on both runtime and quality (Section B.1). Second, we run Algorithm 1 repeatedly to analyze its ability to find global optima (Section B.2). As an overview, the characteristics of the instances of the learning problems we investigate here are available in the following table:

Section	Figure	Source	$ \mathcal{T} $	$ \mathcal{T}_l $	$ \mathcal{L} $	Avg. $T(\phi)$	l_i Boolean	Incons.
<i>B</i> .1	<i>B</i> .1	UW-CSE	2,161	49	339	6.0	yes	yes
B.2	B.2(a)	UW-CSE	2,161	49	113	8.5	yes	no
<i>B.</i> 2	B.2(b)	UW-CSE	2,161	49	339	6.0	yes	yes

B.1 Varying Error Rates

Setup. We use Section A.1's setup with twice as many negative labels as positive ones, where we vary ϵ_{rel} from 10^{-1} to 10^{-5} . Moreover, we set $\epsilon_{abs} := \frac{\epsilon_{rel}}{100}$. In comparison, all other experiments had fixed $\epsilon_{rel} = 10^{-4}$ and $\epsilon_{abs} = 10^{-6}$.

Results. In Figure B.1 we display both runtime and quality in terms of the F_1 measure.

Discussion. While inspecting Figure B.1 we realize that decreasing the error-rates the runtime increases slightly. Furthermore, F_1 is worse for $\epsilon_{rel} > 10^{-3}$. But, if we compare the overall runtime presented in the paper's Figure 4(c), we realize that Algorithm 1 consumes only small portions of the total runtime of about 3 seconds.



Figure B.1: Varying Error Rates



Figure B.2: Finding Global Optima

B.2 Finding Global Optima

Setup. We use Section A.1's setup with two different instances, a consistent one (only positive labels) and an inconsistent one (positive and negative labels).

Results. In Figure B.2 we depict histograms of the resulting mean-squarederror (MSE) of 100 runs on each instance.

Discussion. Algorithm 1 always finds solutions extremely close to the global optimum (0.0) in the consistent instance (Figure B.2(a)). The inconsistent instance, however, has global optima of values larger than 0.0. In this case Algorithm 1 converges very close to a (probably) global optimum in 78% of the runs.

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