

Universität des Saarlandes FR Informatik



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Tutorials for "Logic in Computer Science" Exercise sheet 10

Exercise 10.1:

We define a matching relation between lists (analogously to the matching relation for Unix shell patterns) in the following way:

- every list matches itself.
- the list [*] matches every (possibly empty) list.
- the list [?] matches every list of length 1.
- if l_1 matches l'_1 and l_2 matches l'_2 , then the concatenation of l_1 and l_2 matches the concatenation of l'_1 and l'_2 .

Example: The list [*, one, *, *, 5, ?] matches the list [one, 2, 3, 4, 5, six].

Implement a Prolog predicate matches (XL,YL) that succeeds if and only if the list XL matches the list YL. (Hint: One can implement matches without using append or other auxiliary predicates. If you prefer to use append, beware of non-termination.)

Exercise 10.2:

Give a logical program P such that $T_P^0(\emptyset) \subset T_P^1(\emptyset) \subset T_P^2(\emptyset) \subset T_P^3(\emptyset) = T_P^n(\emptyset)$ for all $n \geq 3$.

Exercise 10.3:

Let $\Sigma = (\{a/0\}, \{p/1, q/1\})$. Show that there exists no Σ -model I of the clause $C = p(a) \vee q(a)$ such that $I \models A \Leftrightarrow C \models A$ for all Σ -atoms A. (In other words: C does not have a canonical model.)

Exercise 10.4:

Prove part (1) of Theorem 2.9:

$$I_P = I_{G_{\Sigma}(P)} = \bigcup_{i=0}^{\infty} T_P^i(\emptyset) = \bigcap_{T_P(I) \subseteq I} I$$

You can use all the preceding theorems.

Exercise 10.5:

Prove the footnote on slide 27: Let Σ be a signature with infinitely many constants. Let P be a set of closed Σ -formulas, let $\forall \vec{x} G$ be a closed Σ -formula (where \vec{x} is the list of all variables occurring in G). Let ρ be a substitution that maps all variables in \vec{x} to pairwise different constants that do not occur in P or G. Then $P \models G\rho$ implies $P \models \forall \vec{x} G$.

Put your solution into the mail box at the door of room 627 in the MPI building (46.1) before June 28, 11:00 (Group D: before July 1, 11:00). Don't forget to write your name and the name of your tutorial group (B, C, D) on your solution.