

Universität des Saarlandes FR Informatik



Harald Ganzinger Uwe Waldmann June 6, 2002

Tutorials for "Logic in Computer Science" Exercise sheet 8

Exercise 8.1:

Compute maximal strict tableaux for the following sets of formulas and explain whether the paths/the tableaux are closed. (Use exactly the expansion rules on Slide 151; don't use shortcuts.)

- (a) $\{\neg((\neg p \to q) \to (p \land q))\}$
- (b) $\{p \lor q, \neg p \lor q, p \lor \neg q, \neg p \lor \neg q\}$

Exercise 8.2:

Theorem 1.48 states that the set of all formulas on a maximal open path of a propositional tableau is satisfiable. The proof of Theorem 1.48 that is given on Slide 156 works only for clausal tableaux. Give a proof for arbitrary propositional tableaux. (Hint: Prove first that the set of all atoms and negated atoms occurring on a maximal open path is satisfiable; then use induction. Omit the subproofs for \rightarrow , \leftarrow , \uparrow , \downarrow .)

Exercise 8.3:

Compute a closed tableau for

$$\left\{ \left(\forall x \, \exists y \, \Big(p(x,x) \, \rightarrow \, \neg p(x,y) \Big) \right) \wedge \left(\exists x \, \forall y \, \, p(x,y) \right) \right\}$$

Exercise 8.4:

Prove the following subcase of Theorem 1.50: If T is a satisfiable tableau, then the tableau T' that results by applying the δ -expansion rule to T is also satisfiable.

Put your solution into the mail box at the door of room 627 in the MPI building (46.1) before June 13, 11:00 (Group D: before June 17, 11:00). Don't forget to write your name and the name of your tutorial group (B, C, D) on your solution.